

FSM limitations (*computational power*)

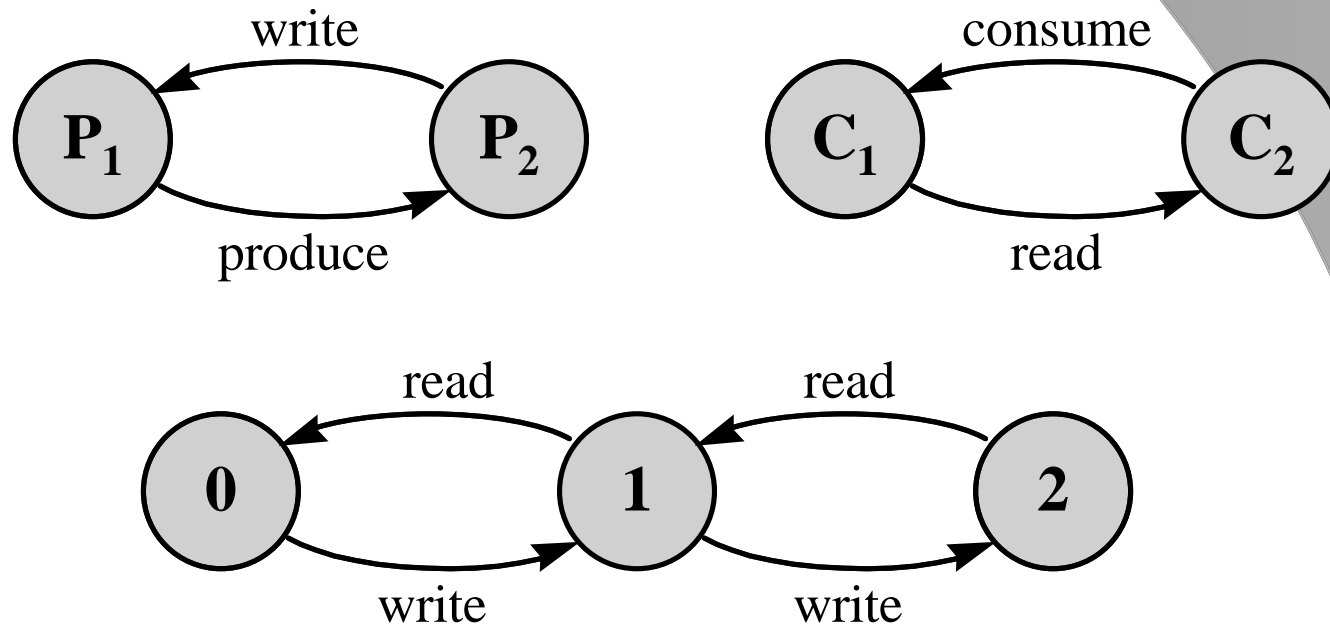
- Consider a car ABS (again) in particular the sub-system that calculates the actual brake pressure required. The range of pressures that can be handled by the servo units is potentially very great.

Therefore defining a state for every possible pressure value that can be required would be unusable!

- Consider modelling the behaviour of a simple 8-bit register - this requires **2^8 distinct states!**

FSM limitations (*state explosion - 1*)

- Consider a typical producer-consumer system modelled using three separate FSMs as follows:



FSM limitations (*state explosion - 2*)

- Integrating parts of one system

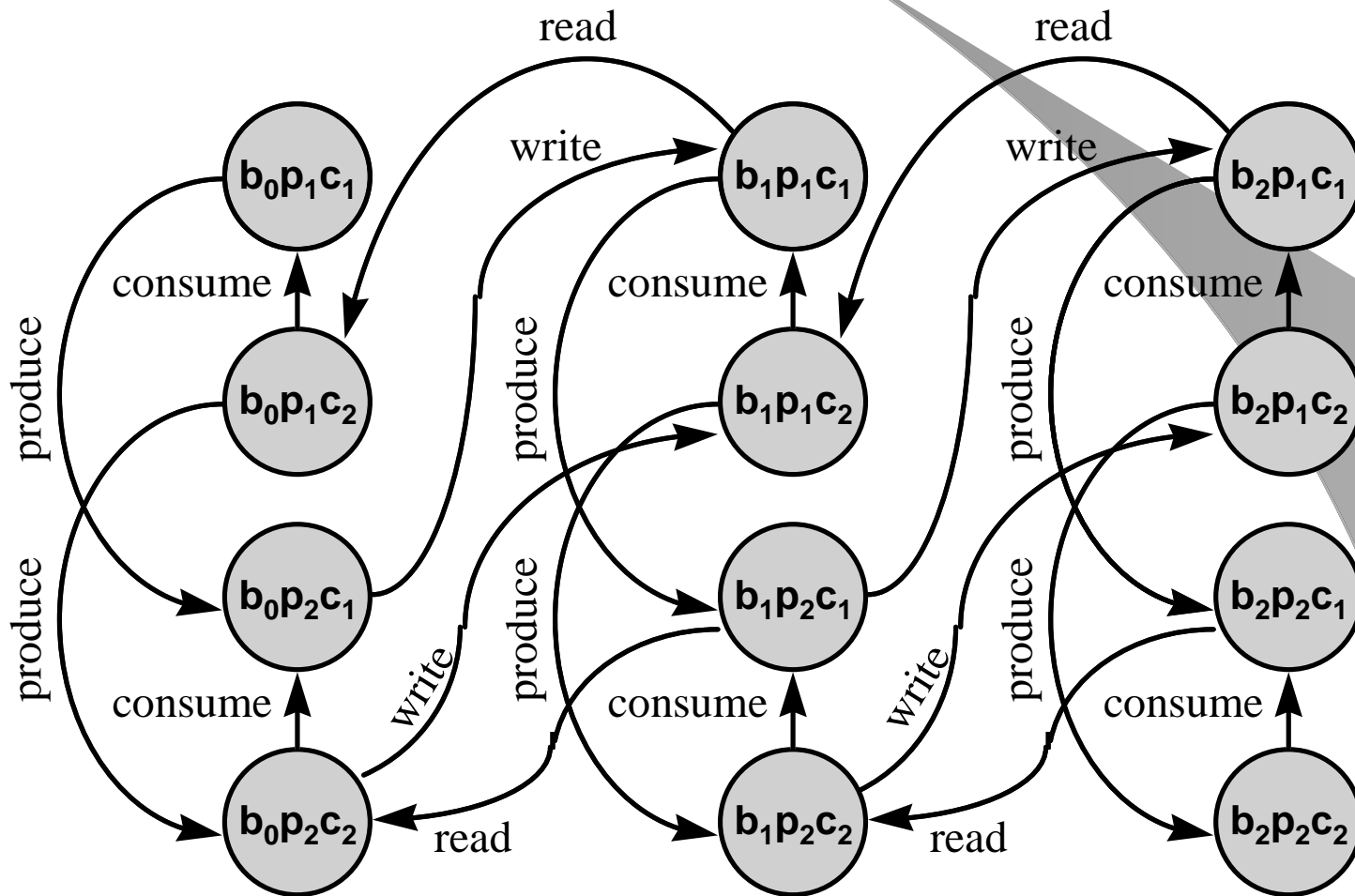
The number of states for a composite FSM made up of **n** sub-systems each with **m_i** states is **m₁ x m₂ x ... m_n**. In the case of the producer-consumer example this would mean the following:

The possible states of P (p₁, p₂) multiplied by the possible states of C (c₁, c₂) multiplied by the possible states of the buffer B - i.e. empty(b₀), one entry(b₁) and two entries(b₂)

**<b₀, p₁, c₁> <b₁, p₁, c₁> <b₂, p₁, c₁>
<b₀, p₁, c₂> <b₁, p₁, c₂> <b₂, p₁, c₂>
<b₀, p₂, c₁> <b₁, p₂, c₁> <b₂, p₂, c₁>
<b₀, p₂, c₂> <b₁, p₂, c₂> <b₂, p₂, c₂> 12 states in all**

FSM limitations (*state explosion - 3*)

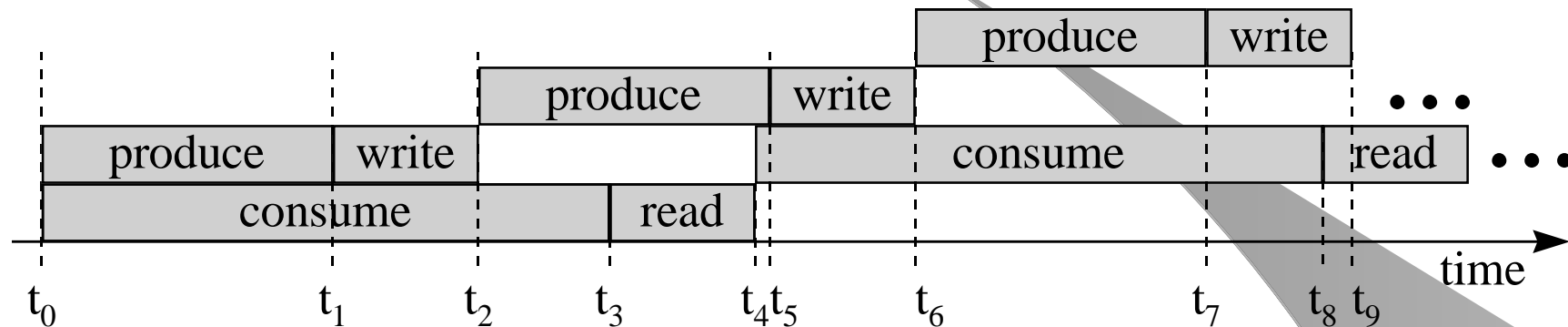
The resulting integrated FSM:



FSM limitations (*modelling timing -1*)

- An FSM is a “snapshot” of a system at a particular instant in time
- An FSM assumes one action (transition) per instant in time
- Asynchronous (i.e. potentially concurrent) actions can be of different duration (*eg. $p = t$; $c = 2t$; $r = w = t/4$*)
- This aspect (concurrent action timing) of system operation is not clearly captured by FSMs

FSM limitations (*modelling timing -2*)



t_0 : $\langle b_0, p_1, c_2 \rangle$	t_5 : $\langle b_0, p_2, c_2 \rangle$
t_1 : $\langle b_0, p_2, c_2 \rangle$	t_6 : $\langle b_1, p_1, c_2 \rangle$
t_2 : $\langle b_1, p_1, c_2 \rangle$	t_7 : $\langle b_1, p_2, c_2 \rangle$
t_3 : $\langle b_1, p_1, c_1 \rangle$	t_8 : $\langle b_1, p_2, c_1 \rangle$
t_4 : $\langle b_0, p_1, c_2 \rangle$	t_9 : $\langle b_1, p_1, c_1 \rangle$

The states at times t_0 and t_4 are the same $\langle b_0, p_1, c_2 \rangle$ as are also the states at times t_1 and t_5 $\langle b_0, p_2, c_2 \rangle$, states t_2 and t_6 $\langle b_1, p_1, c_2 \rangle$, states t_3 and t_9 $\langle b_1, p_1, c_1 \rangle$. However, looking at the graph it is clear that they do not refer to the same actions. This fact is not captured adequately by the FSM.

Petri Net (PN) components

- Graphical formalism of system behaviour specification
- Constituents:
 - finite set of *places* **P**
 - finite set of *transitions* **T**
 - finite set of *directed arcs* **A**
(these connect either places to transitions or vice-versa)
- PN marking - imposing a state on the PN.
- Tokens - used to mark a PN

Petri Nets specs

- Referred to as: **PN**
- To model: **Asynchronous systems**
- Type: **Formalised notation**
- Popularity: **Medium**
- Notation: **Relatively simple and intuitive**



Place symbol



Transition symbol

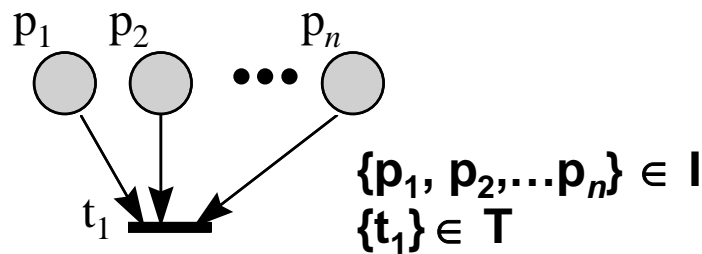


Connecting arc symbol

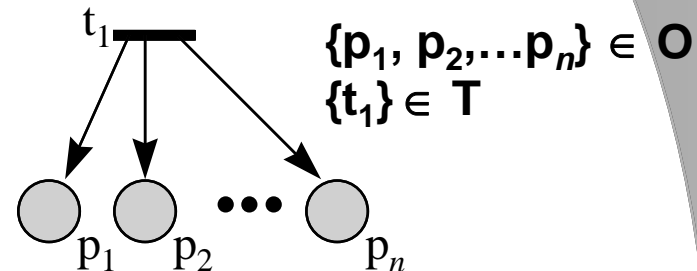
PN “evolution” rules (1)

- PN evolution implies movement of tokens
- A PN does not change shape as it evolves
- A transition may have one or more input or output places

- Input places $\{I\} \subset \{P\}$



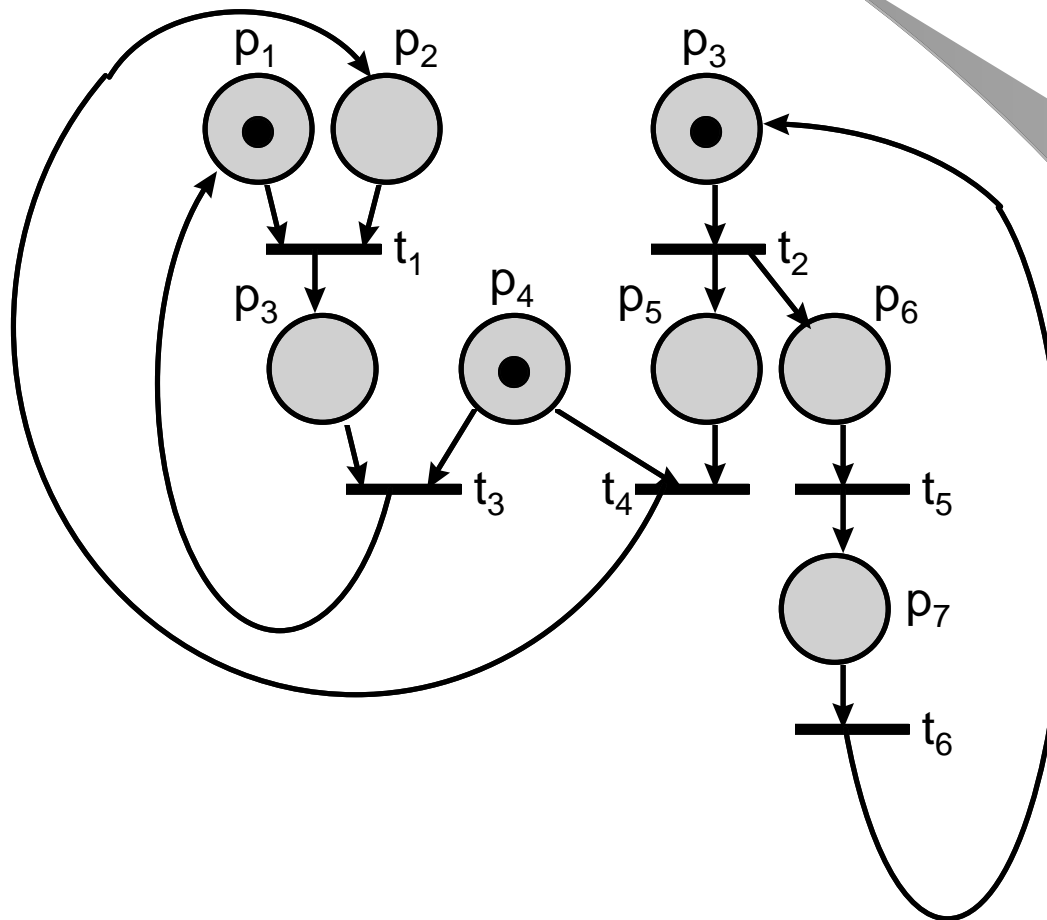
- Output places $\{O\} \subset \{P\}$



PN “evolution” rules (2)

- Transition enabled \Rightarrow
At least **one** token in **each** of transition’s input places.
- Transition “firing” \Rightarrow
Only enabled transitions can fire.
- PN evolution \Rightarrow
Every firing leads to a new PN (i.e. system) state. This is to PN evolution.
- Evolution result (*apart from new state*) \Rightarrow
One token is removed from each input place and **one** is inserted into each output place.

PN example



Some PN modelled situations (1)

- **Firing sequence**

The string of transitions $\langle t_1, t_2, \dots, t_n \rangle$ where t_1 is enabled in the PN's initial marking.

A possibility in the previous example: $\langle t_2, t_4, t_1 \rangle$

- **Nondeterminism**

The possibility of more than one evolution path given an initial marking.

Possibilities in the previous example: $\langle t_2, t_4, t_1 \rangle$

or: $\langle t_2, t_5, t_6, t_2, t_5, t_6, t_2, \dots \rangle$

Some PN modelled situations (2)

- **Deadlock**

In terms of a system modelled using a PN, deadlock is the situation in which no transitions are enabled within a given marking. The PN stops evolving.

- **Livelock**

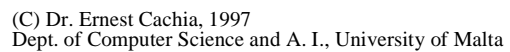
A situation in which deadlock can **never** occur (i.e. the PN will never reach a “conclusive” state).

- **Starvation**

A situation in which part of a system can never proceed due to another part using a resource it needs.

(taken from “Fundamentals of SE” by C. Ghezzi)

Assume this as initial marking.



Deadlock example analysis

- Normal system progress:

The PN evolves according to firing sequence:

$\langle t_1, t_3, t_5, t_7, \dots \rangle$ or

$\langle t_2, t_4, t_6, t_8, \dots \rangle$

- Deadlock situation:

The PN evolves according to firing sequence:

$\langle t_1, t_3, t_2, t_4, d \rangle$ or

$\langle t_2, t_4, t_1, t_3, d \rangle$